

## EXAM 4 - MATH 112

DATE: Tuesday, November 22

INSTRUCTOR: George Voutsadakis

Read each problem very carefully before starting to solve it. Each question is worth 3 points. It is necessary to show your work. Correct answers without explanations are worth 0 points.

**GOOD LUCK!!**

1. Compute the indefinite integrals:

(a)  $\int \frac{x^3+x-3}{x} dx$

(b)  $\int (3x+1)(x^2 + \frac{2}{3}x)^5 dx$

2. Compute the integrals:

(a)  $\int 3xe^{-(x^2+5)} dx$

(b)  $\int \frac{2}{1+e^{3x}} dx$

3. The graph of the function  $f(x) = \frac{x}{(x+3)^3}$  lies above the  $x$ -axis in the interval  $[0, 3]$ . Find the area of the region of the plane that lies between the graph of  $f$  and the  $x$ -axis and the lines  $x = 0$  and  $x = 3$ .
4. Find the area of the region bounded by the graphs of  $f(x) = -x^2 + 4x + 4$ ,  $g(x) = x$ .
5. Find the volume of the solid of revolution formed by revolving the graph of  $f(x) = xe^x$ ,  $0 \leq x \leq 1$ , around the  $x$ -axis.
6. Compute the definite integral  $\int_2^4 \frac{x^4-4}{x^2-1} dx$ .