

## HOMEWORK 4 - MATH 112

DUE DATE: Monday, February 13

INSTRUCTOR: George Voutsadakis

Read each problem very carefully before starting to solve it. One part of each problem will be chosen at random and graded. Each question is worth 1 point. It is necessary to show your work. Correct answers without explanations are worth 0 points.

GOOD LUCK!!

1. A spherical balloon is inflated with gas at a rate of 20 cubic feet per minute. How fast is the radius of the balloon changing at the instant when the radius is 2 feet?
2. A 25-foot ladder is leaning against a house. The base of the ladder is pulled away from the house at the rate of 2 feet per second. How fast is the top of the ladder sliding down the wall when the base is 7 feet from the house?
3. Find the domain, the critical numbers and the open intervals on which the given function is increasing or decreasing.
  - (a)  $f(x) = x^3 - 6x^2$
  - (b)  $g(x) = \sqrt{4 - x^2}$
  - (c)  $f(x) = \frac{2x}{16 - x^2}$
4. Create the table for the first derivative in order to find the monotonicity and the relative extrema of the following functions.
  - (a)  $f(x) = -4x^2 + 4x + 1$
  - (b)  $g(x) = \frac{1}{5}x^5 - x$
  - (c)  $h(x) = x^4 - 32x + 4$
5. Find the absolute extrema of the function in the given closed interval:
  - (a)  $f(x) = x^3 - 12x$  on  $[0, 4]$
  - (b)  $g(x) = \frac{x}{x-2}$  on  $[3, 5]$
6. Use the second derivative test to find all relative extrema of the function. Write "Not Applicable" when the test is inconclusive.
  - (a)  $f(x) = x^4 - 4x^3 + 2$
  - (b)  $g(x) = x + \frac{4}{x}$
  - (c)  $h(x) = \frac{x}{x^2-1}$
7. Make a sign table for both the first and the second derivative to find both the intervals of monotonicity and the intervals of concavity of the following functions.
  - (a)  $f(x) = (x - 1)^3(x - 5)$
  - (b)  $g(x) = (1 - x)(x - 4)(x^2 - 4)$
8. A rectangular page is to contain 30 square inches of print. The margins at the top and at the bottom are to be 2 inches wide. The margins on each side are to be 1 inch wide. Find the dimensions of the page such that the least amount of paper is used.