PRACTICE EXAM 1 - MATH 112

DATE: Tuesday, February 2

INSTRUCTOR: George Voutsadakis

Read each problem very carefully before starting to solve it. Each question is worth 3 points. It is necessary to show your work. Correct answers without explanations are worth 0 points.

GOOD LUCK!!

- 1. Find the following limits:

 - (a) $\lim_{x \to 7} \frac{2x^2 13x 7}{x^2 2x 35}$ (1 point) (b) $\lim_{x \to 2} \frac{x 2}{\sqrt{x + 2} 2}$ (2 points)
- 2. (a) Give the formal (not geometric) definition of a function y = f(x) being continuous at x = a. (1 point)
 - (b) Consider the function

$$f(x) = \begin{cases} 5x - \frac{9}{2}, & \text{if } x < 1\\ 2, & \text{if } x = 1\\ \frac{\sqrt{x-1}}{x-1}, & \text{if } x > 1 \end{cases}$$

Does $\lim_{x\to 1} f(x)$ exist? Explain in detail. (1 point) Is f(x) continuous at x = 1? Explain in detail. (1 point)

- 3. (a) The limit definition of the derivative says that f'(a) = ? (1 point)
 - (b) Use the limit definition of the derivative to compute the derivative of the function f(x) = $3x - \frac{2}{x}$ at the point x = 2. (2 points)
- 4. The height h in feet of an object fired straight up from the ground with an initial velocity of 640 feet per second is given by $h(t) = -16t^2 + 640t$, where t is time in seconds.
 - (a) Find the maximum height that the object will reach and when it will reach that maximum height. (2 points)
 - (b) Find when the object will hit the ground. (1 point)
- 5. Find the derivatives of the functions:
 - (a) $f(x) = (x^4 + \frac{3}{x})(\sqrt[4]{x^7} \frac{2}{\sqrt[3]{x^2}})$ (2 points)
 - (b) $g(x) = \frac{x^5 + 7x 2}{7 x^9}$ (1 point)
- 6. (a) Find the derivative of the function $f(x) = (x+2)(\frac{x-5}{x+1})$. (1.5 points)
 - (b) Find the slope of the tangent line to the graph of y = f(x) at x = 0. (0.5 points)
 - (c) Find the equation to the tangent of y = f(x) at x = 0. (1 point)