

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

Recall that in class we derived the following series formulas (for appropriate convergence intervals):

$$\frac{1}{1-x} = \sum_{n=0}^{\infty} x^n, \quad \cos x = \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n)!} x^{2n}, \quad (1+x)^k = \sum_{n=0}^{\infty} \binom{k}{n} x^n.$$

1. Evaluate the indefinite integral  $\int \frac{x - \tan^{-1} x}{x^3} dx$  as a power series.

2. Obtain a Maclaurin series for the function  $f(x) = x \cos 2x$ .

3. Expand the function  $\frac{1}{(2+x)^3}$  as a power series.