

YOUR NAME: \_\_\_\_\_

George Voutsadakis

Read each problem **very carefully** before starting to solve it. Each problem is worth 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. An open top box with square base is to have a volume of  $500 \text{ in}^3$ . Find the dimensions of the box that can be made with the smallest amount of materials.

2. A hailstone (small sphere of ice) is forming so that its volume is growing at the rate of  $32\pi$   $\text{mm}^3$  per minute. How fast is its radius growing at the moment when its radius is 2 mm? (Formula that gives the volume of a sphere  $V$  as a function of its radius  $r$  is  $V = \frac{4}{3}\pi r^3$ .)

3. The number of welfare cases in a city of population  $p$  is expected to be  $W = 0.003p^{4/3}$ . If the population is growing by 1000 people per year, find the rate at which the number of welfare cases will be increasing when the population is  $p = 1,000,000$ .