

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Determine (if possible) the values of the constants  $a, b$  so that the matrices  $A = \begin{bmatrix} 1 & -2 \\ a & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & 2 \\ 5 & b \end{bmatrix}$  commute under matrix multiplication.

2. Given  $2 \times 2$  matrices  $A, B, C$  the **cancelation law**  $AB = AC \Rightarrow B = C$  does not always hold. Find a counterexample to show this.

3. Determine whether the following matrices  $A, B$  are invertible and, if so, find their inverses.

(a)  $A = \begin{bmatrix} 3 & -5 \\ -2 & 4 \end{bmatrix}$

(b)  $B = \begin{bmatrix} 1 & 0 & -2 \\ -3 & 1 & 4 \\ 2 & -3 & 4 \end{bmatrix}$