## EXAM 3 - CSCI 341 YOUR NAME:

Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. (a) Give the formal inductive definition of the set of regular languages over alphabet A.

- (b) Give a regular expression for the language of all strings over alphabet  $A = \{a, b, c\}$  that start with *abc* or end with *cba*.
- (c) Give a regular expression for the language of all strings over the alphabet  $A = \{0, 1\}$  that do not end with 01.
- (d) Give a formal recursive definition of the operator L that takes as input a regular expression over alphabet A and outputs the regular language that is represented by the given regular expression.

(e) The statement "The language L of all strings over alphabet A = {a, b} that have odd length is regular" is \_\_\_\_\_
Proof:

2. (a) The transition function of a DFA is a function  $\delta : \_ \longrightarrow \_$ , where

- (b) The transition function of an NFA is a function  $\delta$ : \_\_\_\_\_\_, where
- (c) An NFA N accepts a string w over its input alphabet A if, by definition
- (d) Give an NFA that recognizes the regular language  $\{a, b\}^* \{ab\}$ .

(e) Apply the NFA to DFA algorithm to obtain the DFA that corresponds to the NFA you constructed in Part (d).

- 3. (a) Give the form of productions that are allowed in a regular grammar, explaining your symbols.
  - (b) Under each regular expression provide the regular grammar whose language is the same as that represented by the corresponding regular expression:

 $a^* + b^* \qquad ba^* \qquad (aba)^*$ 

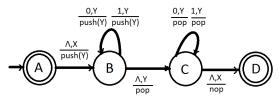
(c) Find a regular grammar for the language represented by the regular expression  $a^*bc^* + ac$ .

(d) Apply the algorithm converting a regular grammar to an NFA to obtain an NFA corresponding to the regular grammar that you gave in Part (c).

4. (a) The PDA instruction  $\langle A, a, X, \mathsf{push}(Y), B \rangle$  can be shown pictorially as follows:

The interpretation of it is that:

- (b) Give the formal definition of an instantaneous description (ID) in a computation of a PDA.
- (c) Consider the following PDA with initial stack symbol X. Give a formal description of an accepting computation on input string 110011 in terms of IDs.



- (d) "The language accepted by the PDA of Part (c) is the language of palindromes over  $A = \{0, 1\}$ " is \_\_\_\_\_ proof:
- (e) Give a PDA that recognizes the language  $\{a^{n+1}b^n a : n \ge 1\}$  (make sure to state which mode of acceptance your PDA is using).

- 5. (a) Give an example of a language that is context-free but not regular (write formally).
  - (b) Apply the relevant algorithm to construct a PDA that accepts the context-free language described by

$$\begin{split} S &\to ABA \\ A &\to aA | \Lambda \\ B &\to bB | \Lambda. \end{split}$$

(c) Apply the relevant algorithm to eliminate  $\Lambda$ -productions from the following grammar:

$$\begin{split} S &\to aSA|bsB|A\\ A &\to aBb|bBa\\ B &\to aB|bB|\Lambda \end{split}$$

(d) Apply the relevant algorithm to produce the Chomsky Normal Form of the following context-free grammar.

 $\begin{array}{l} S \rightarrow C \\ C \rightarrow a C a | b C b | A \\ A \rightarrow a B b | b B a \\ B \rightarrow a B | b B | b \end{array}$