Read each problem very carefully before starting to solve it. Each problem is worth 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Give the formal inductive definition of the set $\mathcal{R}$ of regular expressions:

## Basis:

## Induction:

2. Apply the operator $L$ that associates to a given regular expression the corresponding regular language recursively (showing all steps) to discover the regular language $L\left(b\left(a^{*} b c^{*}+a c\right)\right.$ ):
$L\left(b\left(a^{*} b c^{*}+a c\right)\right)=$
3. Write a regular expression for the language $L$ over the alphabet $A=\{a, b, c\}$ consisting of all strings that contain the substring $a b a$ and end in $c$.
4. The equation $(R R)^{*}=R^{*} R^{*}$ between regular expressions is $\qquad$
Proof:
