Read each problem very carefully before starting to solve it. Each problem is worth 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Use the top-down algorithm to construct an NFA for the regular language described by the regular expression $a^{*}+a b^{*}$ (show one step at a time; so you must execute 4 steps).
2. In the process of obtaining a regular expression for the regular language accepted by an NFA, a colleague of yours has obtained the following diagram:


An emergency has interrupted his work and you are called to continue the process. Execute the remaining two steps by eliminating first State 1 and then State 2 to get the final regular expression (you do not have to simplify after each step).
3. Use the algorithm described in class to get a DFA accepting the same regular language that is accepted by the NFA shown in the following picture. Please carry out one step at a time.


