## EXAM 2 - MATH 152 YOUR NAME:\_\_\_\_\_

Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Find the volume of the solid obtained by rotating the region bounded by the curves  $y = x^2$ and  $x = y^2$  about the line x = -1.

2. Find the volume of the solid generated by rotating the region bounded by the curves  $y = e^{-x^2}$ , y = 0, x = 0 and x = 1 about the y-axis.

3. Calculate the length of the curve  $x = \frac{1}{3}\sqrt{y}(y-3), 1 \le y \le 9$ .

4. A water tank has the shape of the bottom half of a hemisphere with radius 5 feet. If it is full of water that weighs  $62.5 \text{ lb/ft}^3$ , find the work required to pump the water out of the tank (from the top).

5. Find the solution of the differential equation  $\frac{dy}{dx} = \frac{y \cos x}{1 + y^2}$ , that satisfies the initial condition y(0) = 1.