

YOUR NAME: \_\_\_\_\_

George Voutsadakis

Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Find the area of the parallelogram with vertices  $K(1, 2, 3)$ ,  $L(1, 3, 6)$ ,  $M(3, 8, 6)$  and  $N(3, 7, 3)$ .

2. Determine whether the points  $A(1, 3, 2)$ ,  $B(3, -1, 6)$ ,  $C(5, 2, 0)$  and  $D(3, 6, -4)$  lie in the same plane.

3. Find an equation of the plane that passes through the line of intersection of the planes  $x - z = 1$  and  $y + 2z = 3$  and is perpendicular to the plane  $x + y - 2z = 1$ .

4. Find the distance between the parallel planes  $3x + 6y - 9z = 4$  and  $x + 2y - 3z = 1$ .

5. Find the unit tangent vector  $\mathbf{T}(t)$  at the point of the curve  $\mathbf{r}(t) = \cos 3t\mathbf{i} + \sin 4t\mathbf{j} + t\mathbf{k}$ , with  $t = \frac{\pi}{2}$ .

