

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. (**Pollution**) The carbon monoxide level in a city  $t$  years from now is predicted to be

$$P(t) = 0.02\sqrt{(12 + 2t)^3} + 1 \text{ ppm (parts per million).}$$

Find  $P'(2)$ , state its units and interpret your answer.

2. Consider the function

$$f(x) = -x^4 - 4x^3 - 4x^2 + 1.$$

(a) Compute the first derivative and find the critical points of  $f$ .

(b) Create the sign table for  $f'(x)$  and show clearly the intervals where  $f(x)$  is increasing/decreasing and the relative extrema (maxima/minima).

(c) Sketch the graph of  $f(x)$ . Your graph should be **clean** and all points of interest should be **labeled**.