

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Compute the following derivatives:

(a)  $[x^2e^{3x} - (3x + \ln x)^7]' =$

(b)  $\left[ \frac{3e^{5x}}{1 + e^{-2x}} \right]' =$

2. Compute the integrals:

(a)  $\int \frac{2x^5 + x^3e^{9x} - x^2}{x^3} dx =$

(b)  $\int \frac{6x^3 + \sqrt{x^3} - 1}{\sqrt{x^5}} dx =$

3. The price of an ice-cream cone at a certain store in the Soo is increasing at the rate of  $18e^{0.1t}$  cents per year, where  $t$  is the number of years since the store's opening in 2010.

(a) If in 2010, when the store opened, the price was set at \$4.00, what would the price be  $t$  years after 2010?

(b) Assuming the store stays open in the foreseeable future, when is the price of the ice-cream cone predicted to reach \$7.00?

4. A model giving the sales of apple computers immediately following the turn of the millennium is

$$S(x) = 2x^2 - 9x + 39 \text{ hundreds thousands.}$$

where  $x$  is the number of years since 2000.

What were the average sales from 2000 to 2006?

5. Find the area of the region enclosed by the graphs of  $f(x) = x^3$  and  $g(x) = 4x$ .