Read each problem very carefully before starting to solve it. Each problem is worth 10 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Solve the equations:
(a) $6 x^{3}=2 x-11 x^{2}$
(b) $(x+2)(x+3)=20$
2. Solve the equation $\left|x^{2}+2 x-19\right|=16$.
3. Perform the operations and simplify:
(a) $\frac{8 x}{2 x^{2}+4 x+2}-\frac{3 x-3}{x^{2}-1}=$
(b) $\frac{\frac{3}{x+2}-\frac{4}{x^{2}-4}}{\frac{1}{x-2}-\frac{3}{x+2}}=$
4. Jayne can paint a 2-bedroom house by herself in $x$ days. Alma, slower and more deliberate, takes four more days than Jayne to paint a 2-bedroom house by herself.
(a) Write a function $P(x)$ for the number of 2-bedroom houses that Jayne and Alma can paint working together as a team in a month (30 days).
(b) Compute how many 2-bedroom houses they can paint together in a month, if Jayne can paint a 2-bedroom house by herself in 6 days.
5. (a) Divide $\left(3 x^{3}+x^{2}-7 x+6\right) \div(3 x-5)$ and write your answer in the form

$$
\frac{\text { divident }}{\text { divisor }}=\text { quotient }+\frac{\text { remainder }}{\text { divisor }}
$$

(b) Use division to find the value $P(4)$ if $P(x)=-x^{3}+5 x^{2}+3 x$.

