Read each problem very carefully before starting to solve it. Each problem is worth 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Consider the quadratic function $f(x)=-x^{2}-2 x+3$.
(a) Find its vertex.
(b) Find the opening direction.
(c) Find its $y$-intercept.
(d) Find its $x$-intercept(s).
(e) Sketch the graph of the function, labeling all points of interest.
2. A friend of yours has set up a small home operation producing a certain type of gadget. Each gadget costs her $\$ 100$ and her fixed costs are $\$ 220$. If she produces and sells $x$ gadgets, she has found that the price that she can charge per gadget is $(132-x)$ dollars.
(a) Find the cost function of your friend's operation.

$$
C(x)=
$$

(b) Find the revenue function of your friend's operation.

$$
R(x)=
$$

(c) Find the profit function of your friend's operation.

$$
P(x)=
$$

(d) How many gadgets does your friend have to sell in order to maximize her profit?
(e) At which production level(s) does your friend's operation break even?

