Read each problem very carefully before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [3 points] Show from scratch that $\mathcal{L}\left\{y^{\prime}\right\}=s F(s)-f(0)$, where $F(s)=\mathcal{L}\{y\}$.
2. [3 points] Compute from scratch the Laplace transform of $u_{c}(t)$.
3. [6 points] Use Laplace transforms to find the particular solution of the initial value problem

$$
2 y^{\prime \prime}+7 y^{\prime}+3 y=0, \quad y(0)=-1, \quad y^{\prime}(0)=8
$$

