Friday, September 22 George Voutsadakis

Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Compute the area of the region enclosed by the graphs of $f(x) = x^3 + x$ and g(x) = 2x. Please, show all steps. 2. Consider the solid whose floor is the region bounded by $x = 4 - y^2$ in the first quadrant and whose cross-sections perpendicular to the *y*-axis are squares. Find the volume of this solid.

3. Find the volume of the solid resulting by rotating the region under the graphs of $y = \cos x$, $0 \le x \le \frac{\pi}{2}$, around the *y*-axis.

4. Compute the integral $\int x^{-6} \ln x dx$.

5. Compute the integral $\int \tan^3 x \sec^7 x dx$.