Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

- 1. [4 points] Do the following:
  - (a) Suppose a sequence  $a_n$  is defined recursively by

$$a_0 = 5, \quad a_{n+1} = \frac{1}{3}a_n.$$

Find a (non-recursive) formula for  $a_n$  in terms of n.

(b) Suppose  $a_n = 5n - 1$ . Find a recursive formula for  $a_n$  in terms of  $a_{n-1}$ .

2. [4 points] Compute the limit of the sequence  $a_n = \frac{5n \log n}{n \log n + n^2}$ . (Show all steps!)

2. [4 points] Compute the limit of the sequence  $c_n = \frac{2n^2 + 7}{5n^2 + 2n} - 3\left(-\frac{2}{3}\right)^n$ . (Show all steps!)