Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

- 1. [6 points] Consider the differential equation y'' 6y' + 9y = 0.
  - (a) Verify that  $y_1(t) = e^{3t}$  is one of its solutions.

(b) Use Abel's Formula to compute  $W(y_1, y_2)(t)$  (leaving in the undetermined constant).

(c) Using the result of Part (b) and the fact that you know  $y_1(t) = e^{3t}$  try to determine the form of  $y_2(t)$ .

2.  $[6 \ {\rm points}]$  Consider the initial value problem

$$y'' + 2y' + 50y = 0, \quad y(0) = 1, \quad y'(0) = 10.$$

Find its particular solution (expressed in terms of real functions).