Read each problem very carefully before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Use Laplace transforms to solve the initial value problem

$$
y^{\prime \prime}+y^{\prime}=e^{-t}, \quad y(0)=1, \quad y^{\prime}(0)=0
$$

2. [4 points] Compute from scratch (without the use of the table) the Laplace transform of

$$
f(t)=u_{3}(t) e^{-t}+u_{5}(t)\left(t-e^{-t}\right)-u_{8}(t) t .
$$

3. [4 points] Compute the Laplace transform of

$$
f(t)=\left\{\begin{array}{lll}
\sin t, & \text { if } \quad 0 \leq t<\pi \\
\sin t+\cos t, & \text { if } \quad \pi \leq t<2 \pi \\
2 \sin t+\cos t, & \text { if } t \geq 2 \pi
\end{array}\right.
$$

