Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Use Laplace transforms to solve the initial value problem

$$y'' + y' = e^{-t}, \quad y(0) = 1, \quad y'(0) = 0.$$

 $2. \ [4 \ {\rm points}]$ Compute from scratch (without the use of the table) the Laplace transform of

$$f(t) = u_3(t)e^{-t} + u_5(t)(t - e^{-t}) - u_8(t)t.$$

3. [4 points] Compute the Laplace transform of

$$f(t) = \begin{cases} \sin t, & \text{if } 0 \le t < \pi\\ \sin t + \cos t, & \text{if } \pi \le t < 2\pi\\ 2\sin t + \cos t, & \text{if } t \ge 2\pi \end{cases}$$