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Read each problem very carefully before starting to solve it. Each problem is worth 10 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Consider the polynomial $f(x)=x^{3}-3 x+2$.
(a) Note that $f(1)=0$. Use the Factor Theorem to find all factors of $f(x)$.
(b) Based on Part (a) give all zeros of $f(x)$ and their multiplicities.
(c) Based on Part (b), sketch the graph of $y=f(x)$. (Please, be neat and label all important points.)
2. The following figure show the graph of a polynomial function $y=f(x)$.

(a) Describe formally the end behavior of $y=f(x)$.
(b) Give the zeros and their multiplicities.
(c) Find a formula for $y=f(x)$.
3. The following figure shows the graph of a rational function $y=f(x)$.

(a) Find the vertical and horizontal asymptotes (these are lines).
(b) Find the $x$ - and $y$-intercepts (these are points).
(c) Find a possible formula for $y=f(x)$.
4. Consider the function $f(x)=2(x-3)^{2}-1$.
(a) Sketch its graph neatly, labeling all important points.
(b) Restrict its domain so as to be able to consider an inverse function.
(c) Find a formula for the inverse of $f(x)$, assuming its domain is the one you gave in Part (b).
5. Suppose a quantity $x$ varies

- directly with both $y$ and the cube root of $z$;
- inversely with the square of $w$.
(a) Write an equation expressing the relation of joint variation described above (with undetermined constant).
(b) Suppose that, when $y=2, z=27, w=2$, we have $x=9$. Determine the constant you used in Part (a).
(c) Find the value of $z$, if $x=24, y=12$ and $w=3$.

