Read each problem very carefully before starting to solve it. Each problem is worth around 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Divide $\left(x^{4}-x^{3}\right) \div\left(x^{2}+1\right)$ and write your answer in the appropriate form.
2. [5 points] Let $f(x)=\frac{2 x-4}{3 x+1}$. Find by hand the following:
(a) The domain of $f$.
(b) The vertical asymptote(s) (these are line(s)).
(c) The horizontal asymptote (this is a line).
(d) The $y$-intercept (this is a point).
(e) The $x$-intercept(s) (these are point(s)).
3. [5 points] The graph of $y=f(x)$ is shown below. Answer the following questions referring to the graph.

(a) Find the vertical asymptote(s).
(b) Find the horizontal asymptote.
(c) Find the $x$-intercept(s).
(d) Find the $y$-intercept.
(e) Give a formula for $y=f(x)$.
