Read each problem very carefully before starting to solve it. Each problem is worth around 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Compute the integral $\int \frac{x^{5}-x^{2} e^{7 x}+x-1}{x^{2}} d x$.
2. [4 points] Sketch the region trapped between the graph of $f(x)=4-x^{2}$ and the $x$-axis and find its exact area.
3. [4 points] Find the average value of the function $f(x)=\frac{3}{x}$ on the interval $\left[\frac{1}{e}, e\right]$. Please, provide an exact expression (without decimals).
