

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

- (a) Using a small table of values, sketch the graph of the exponential function  $f(x) = 2^x$ .

- (b) Fill in the blank spaces with appropriate equations reflecting the transformations described inside the parentheses on the right.

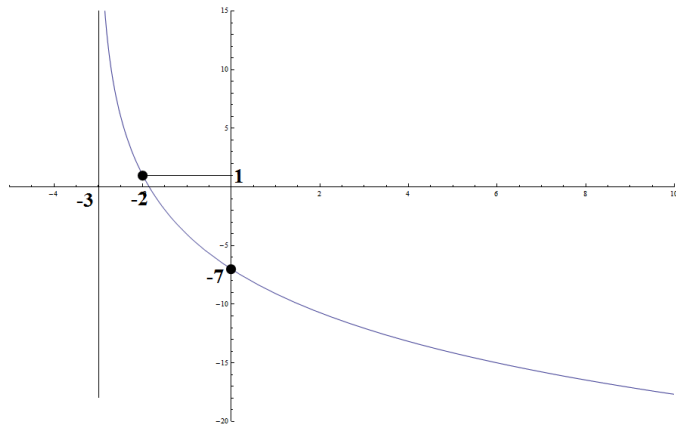
$$y = 2^x \longrightarrow \text{(shift down by 3)}$$

$$\longrightarrow \text{(shift left by 1)}$$

$$\longrightarrow \text{(vertical compression by a factor of 5)}$$

After these transformations, the horizontal asymptote is:

2. The following graph shows a transform of the logarithmic function with base 5. Find a formula of the function whose graph is shown, explaining one-by-one all your steps.



3. Expand or combine as appropriate, using properties of logarithms:

(a)  $\ln\left(\frac{x^2y^7}{z^3}\right) =$

(b)  $2\log x + 5\log y - \frac{1}{3}\log z =$

4. Solve the following equations:

(a)  $6e^{9x+8} + 2 = -74$

(b)  $10 - 4\ln(9 - 8x) = 6$

5. Solve the following equations:

(a)  $3^{2x-1} = 7^{x-2}$ .

(b)  $\log(x + 3) - \log x = \log 74$ .