Read each problem very carefully before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [3 points] Use long division and write your answer in an appropriate form:

$$
\left(3 x^{5}+5 x^{2}-1\right) \div\left(x^{2}+1\right)
$$

2. [3 points] Use synthetic division and write your answer in an appropriate form:

$$
\left(3 x^{4}-x^{2}+5 x-2\right) \div(x+2)
$$

3. [3 points] Use the Remainder Theorem to compute $f(2)$, where $f(x)=x^{3}+2 x^{2}-7$.
4. [3 points] Find by inspection a root of the polynomial $f(x)=3 x^{3}+17 x^{2}-27 x+7$. Then, use the root you found, together with the Factor Theorem, to find the remaining roots of the polynomial. (Please, describe what you are doing as you proceed.)
