Read each problem very carefully before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [6 points] Consider the function $d_{1}(t-7)$.
(a) Define it formally on the left and sketch its graph (neatly) on the right below.
(b) Compute from scratch the Laplace transform $\mathcal{L}\left\{d_{1}(t-7)\right\}$.
2. [6 points] Solve using Laplace Transforms the initial value problem

$$
y^{\prime \prime}+9 y=27 \delta(t-7), \quad y(0)=3, y^{\prime}(0)=1 .
$$



