Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Consider the function

$$f(x) = -x^3(x+1)(x-2)^2.$$

- (a) Identify formally its end-behavior showing all steps.
- (b) Find its *x*-intercepts together with their multiplicities.
- (c) Use the data gathered to sketch its graph labeling all important points.

2. [4 points] Consider the graph of y = f(x) shown.



- (a) Identify the end-behavior.
- (b) Find the x intercepts and their multiplicities.
- (c) Find a formula for the function y = f(x).

3. [4 points] Perform the synthetic division and write your answer in an appropriate form.

$$(x^4 - x^3 + 3x^2 + 1) \div (x+2).$$