Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Convert from exponentials to logarithms or vice-versa as appropriate.

 $y = \log_7 (10) \longrightarrow$ $x = e^{23} \longrightarrow$ $7 = \log a \longrightarrow$ $5^y = 29 \longrightarrow$

2. [2 points] Use a small table of values to sketch the graph of $y = \log_{\frac{1}{2}} x$.

3. [4 points] Detect the transformations needed to get from $f(x) = \log_3 x$ to

$$g(x) = \log_3{(5-x)} + 7.$$

$$y = \log_3 x \longrightarrow ()$$

$$\longrightarrow \qquad ()$$

$$\longrightarrow \qquad y = \log_3 (5 - x) + 7 \qquad ()$$

4. [4 points] The following shows the graph of a transform y = f(x) of the logarithm to base 5. Find a possible formula for y = f(x) showing (and explaining) all your steps.

