Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

- 1. [6 points]
  - (a) Write a second order linear homogeneous differential equation with constant coefficients, whose general solution is  $y(t) = c_1 e^{4t} + c_2 t e^{4t}$ . Please explain the thought process.

(b) Find the particular solution of  $y'' - 3y' + \frac{9}{4}y = 0$ , y(0) = 12, y'(0) = 33.

 $2.\ [6 \ {\rm points}]$  Consider the second order linear homogeneous differential equation

$$t^2y'' + 2ty' - 2y = 0.$$

(a) Verify that  $y_1(t) = t$  is a solution.

(b) Use reduction of order, showing all steps, to obtain a second solution  $y_2(t)$ .