Thursday, March 21 George Voutsadakis

Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [6 points] Consider the function

$$f(t) = \left\{ \begin{array}{ll} 1, & \text{if } 0 \leq t < 2 \\ \frac{1}{2}t, & \text{if } t \geq 2. \end{array} \right.$$

(a) Sketch the graph of y = f(t).

(b) Compute from scratch $\mathcal{L}{f}$.

 $2.\ [6 \ {\rm points}]$ Use Laplace transforms to solve the initial value problem

$$y'' + y = e^t$$
, $y(0) = 5$, $y'(0) = 0$.