Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [2 points] Suppose that, in solving the system  $\mathbf{x}' = A\mathbf{x}$ , you found a complex eigenvalue  $\rho = \lambda + i\mu$  and an associated eigenvector  $\boldsymbol{\xi} = \mathbf{a} + i\mathbf{b}$ . Show the steps to rewrite the part of the solution corresponding to this eigenvalue (without the preceding constant) in real form.

2. [5 points] Solve the system  $\mathbf{x}' = \begin{pmatrix} 5 & -10 \\ -2 & 1 \end{pmatrix} \mathbf{x}$ .

3. [5 points] Solve the system  $\mathbf{x}' = \begin{pmatrix} 1 & -1 \\ 1 & 3 \end{pmatrix} \mathbf{x}$ .