Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [5 points] Consider the function

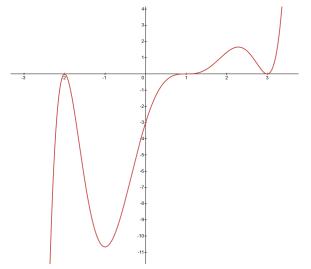
$$f(x) = x^3(x+2)^2(x-3).$$

(a) Give formally the end behavior with some explanations.

(b) Give the *x*-intercepts with their multiplicities.

(c) Make a sketch of the graph using the information in the preceding parts (please, draw it neatly).

3. [7 points] Consider the graph shown in the following figure.



- (a) Give formally its end behavior.
- (b) Find the *y*-intercept.
- (c) Find the *x*-intercepts with their multiplicities.
- (d) Find a possible formula for the function whose graph is shown.